

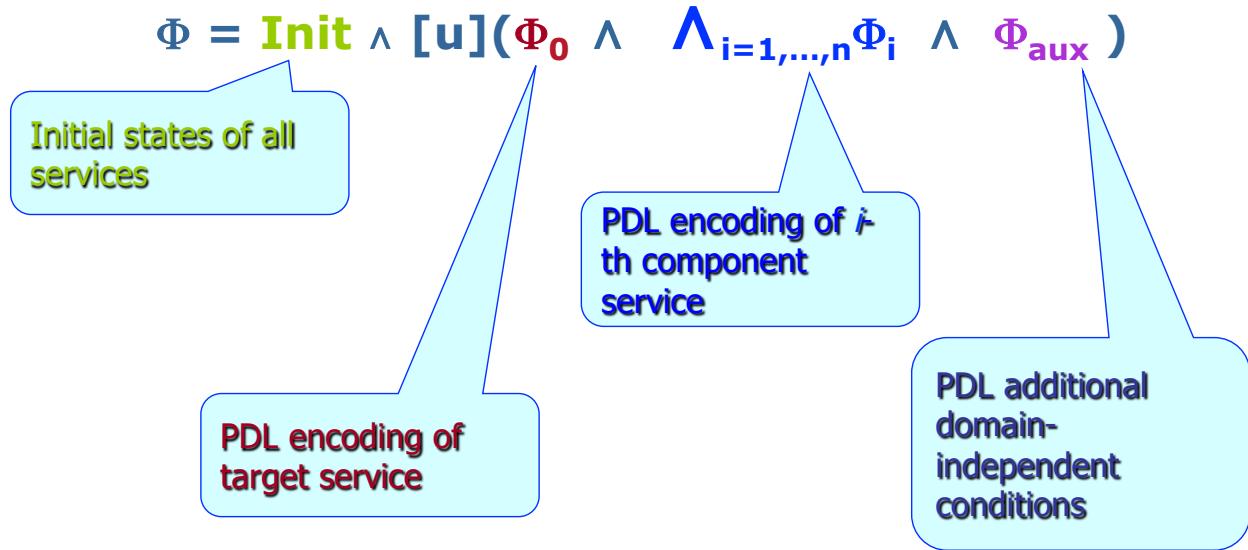
## **Composition: the “Roman” Approach Reduction to SAT in PDL**

### **Encoding in PDL**

Basic idea:

- A orchestrator program  $P$  realizes the target service  $T$  iff at each point:
  - $\forall$  transition labeled  $a$  of the target service  $T$  ...
    - ...  $\exists$  an available service  $B_i$  (the one chosen by  $P$ ) that can make an  $a$ -transition, realizing the  $a$ -transition of  $T$
- Encoding in PDL:
  - $\forall$  transition labeled  $a$  ...
    - use **branching**
  - $\exists$  an available service  $B_i$  that can make an  $a$ -transition ...
    - use underspecified predicates **assigned through SAT**

# Structure of the PDL Encoding



PDL encoding is polynomial in the size of the service TSs

## PDL Encoding

- Target service  $S_0 = (\Sigma, S_0, s^0_0, \delta_0, F_0)$  in PDL we define  $\Phi_0$  as the conjunction of:
  - $s \rightarrow \neg s'$  for all pairs of distinct states in  $S_0$   
*service states are pair-wise disjoint*
  - $s \rightarrow \langle a \rangle T \wedge [a]s'$  for each  $s' = \delta_0(s, a)$   
*target service can do an a-transition going to state s'*
  - $s \rightarrow [a] \perp$  for each  $\delta_0(s, a)$  undef.  
*target service cannot do an a-transition*
  - $F_0 \equiv \vee_{s \in F_0} s$   
*denotes target service final states*
  - ...

## PDL Encoding (cont.d)

- available services  $S_i = (\Sigma, S_i, s^0_i, \delta_i, F_i)$  in PDL we define  $\Phi_i$  as the conjunction of:
  - $s \rightarrow \neg s'$  for all pairs of distinct states in  $S_i$   
*Service states are pair-wise disjoint*
  - $s \rightarrow [a](\text{moved}_i \wedge s' \vee \neg \text{moved}_i \wedge s)$  for each  $s' = \delta_i(s, a)$   
*if service moved then new state, otherwise old state*
  - $s \rightarrow [a](\neg \text{moved}_i \wedge s)$  for each  $\delta_i(s, a)$  undef.  
*if service cannot do a, and a is performed then it did not move*
  - $F_i \equiv \vee_{s \in F_i} s$  denotes available service final states
- ...

## PDL Encoding (cont.d)

- Additional assertions  $\Phi_{aux}$ 
  - $\langle a \rangle T \rightarrow [a] \vee_{i=1, \dots, n} \text{moved}_i$  for each action a  
*at least one of the available services must move at each step*
  - $F_0 \rightarrow \wedge_{i=1, \dots, n} F_i$  when target service is final all comm. services are final
  - $\text{Init} = s^0_0 \wedge_{i=1, \dots, n} s^0_i$  Initially all services are in their initial state

$$\text{PDL encoding: } \Phi = \text{Init} \wedge [u](\Phi_0 \wedge \bigwedge_{i=1, \dots, n} \Phi_i \wedge \Phi_{aux})$$

# Results

## Thm[ICSOC' 03,IJCIS' 05]:

Composition exists iff PDL formula  $\Phi$  SAT

*From composition labeling of the target service one can build a tree model of the PDL formula and viceversa*

*Information on the labeling is encoded in predicates moved,*

## Corollary [ICSOC' 03,IJCIS' 05]:

Checking composition existence is decidable in **EXPTIME**

## Thm[Muscholl&Walukiewicz FoSSaCS'07]:

Checking composition existence is **EXPTIME-hard**

# Results on TS Composition

## Thm[ICSOC' 03,IJCIS' 05]:

If composition exists then finite TS composition exists.

*From a small model of the PDL formula  $\Phi$ ,  
one can build a finite TS machine*

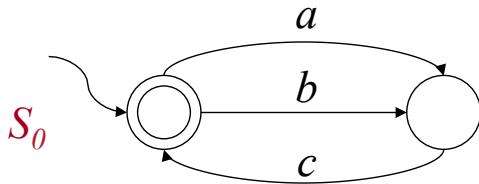
*Information on the output function of the machine is encoded in predicates moved,*

⇒ finite TS composition existence of services expressible as finite TS is EXPTIME-complete

## Example (1)



Target service



PDL

...  
...  
...

$$s_0^0 \wedge s_1^0 \wedge s_2^0$$

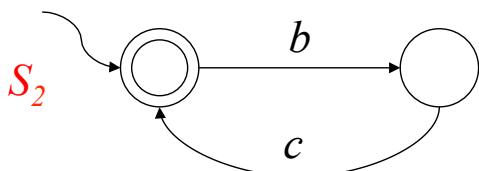
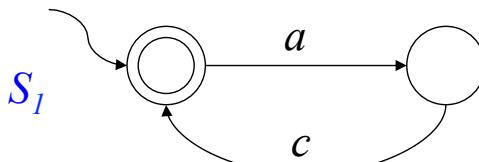
$$\langle a \rangle T \rightarrow [a] (\text{moved}_1 \vee \text{moved}_2)$$

$$\langle b \rangle T \rightarrow [b] (\text{moved}_1 \vee \text{moved}_2)$$

$$\langle c \rangle T \rightarrow [c] (\text{moved}_1 \vee \text{moved}_2)$$

$$F_0 \rightarrow F_1 \wedge F_2$$

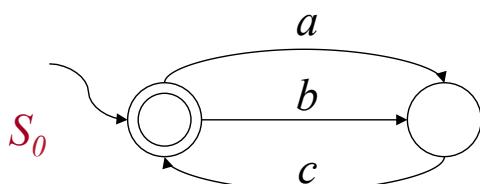
Available services



## Example (2)



Target service



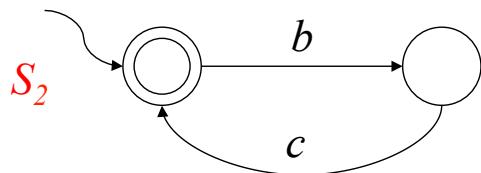
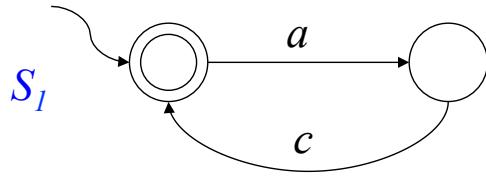
$$\begin{aligned} s_0^0 &\rightarrow \neg s_0^1 \\ s_0^0 &\rightarrow \langle a \rangle T \wedge [a] s_0^1 \\ s_0^0 &\rightarrow \langle b \rangle T \wedge [b] s_0^1 \\ s_0^1 &\rightarrow \langle c \rangle T \wedge [c] s_0^0 \\ s_0^0 &\rightarrow [c] \perp \\ s_0^1 &\rightarrow [a] \perp \\ s_0^1 &\rightarrow [b] \perp \\ F_0 &\equiv s_0^0 \end{aligned}$$

...  
...  
...

## Example (3)



### Available services



...

$$\begin{aligned}
 s_1^0 &\rightarrow \neg s_1^1 \\
 s_1^0 &\rightarrow [a] (\text{moved}_1 \wedge s_1^1 \vee \neg \text{moved}_1 \wedge s_1^0) \\
 s_1^0 &\rightarrow [c] \neg \text{moved}_1 \wedge s_1^0 \\
 s_1^0 &\rightarrow [b] \neg \text{moved}_1 \wedge s_1^0 \\
 s_1^1 &\rightarrow [a] \neg \text{moved}_1 \wedge s_1^1 \\
 s_1^1 &\rightarrow [b] \neg \text{moved}_1 \wedge s_1^1 \\
 s_1^1 &\rightarrow [c] (\text{moved}_1 \wedge s_1^0 \vee \neg \text{moved}_1 \wedge s_1^1) \\
 F_1 &= s_1^0
 \end{aligned}$$

...

$$\begin{aligned}
 s_2^0 &\rightarrow \neg s_2^1 \\
 s_2^0 &\rightarrow [b] (\text{moved}_2 \wedge s_2^1 \vee \neg \text{moved}_2 \wedge s_2^0) \\
 s_2^0 &\rightarrow [c] \neg \text{moved}_2 \wedge s_2^0 \\
 s_2^0 &\rightarrow [a] \neg \text{moved}_2 \wedge s_2^0 \\
 s_2^1 &\rightarrow [b] \neg \text{moved}_2 \wedge s_2^1 \\
 s_2^1 &\rightarrow [a] \neg \text{moved}_2 \wedge s_2^1 \\
 s_2^1 &\rightarrow [c] (\text{moved}_2 \wedge s_2^0 \vee \neg \text{moved}_2 \wedge s_2^1) \\
 F_2 &= s_2^0
 \end{aligned}$$

...

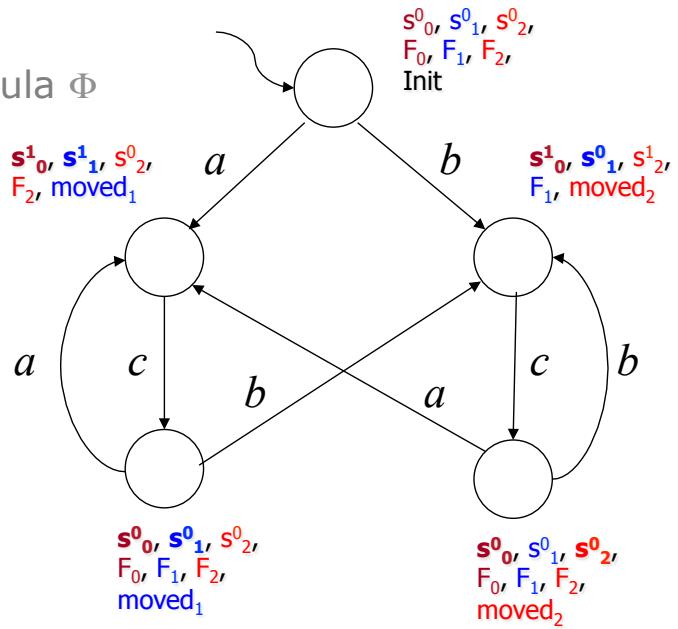
## Example (4)



Check: run SAT on PDL formula  $\Phi$

## Example

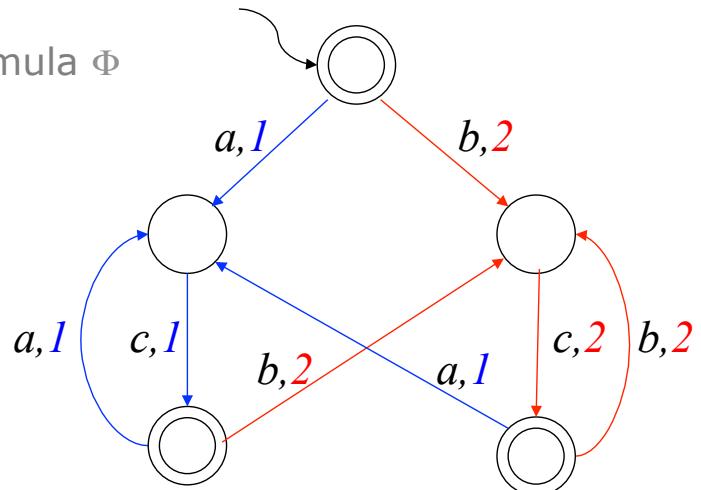
Check: run SAT on PDL formula  $\Phi$   
Yes  $\Rightarrow$  (small) model



## Example

Check: run SAT on PDL formula  $\Phi$   
Yes  $\Rightarrow$  (small) model

$\Rightarrow$  extract finite TS



## Example

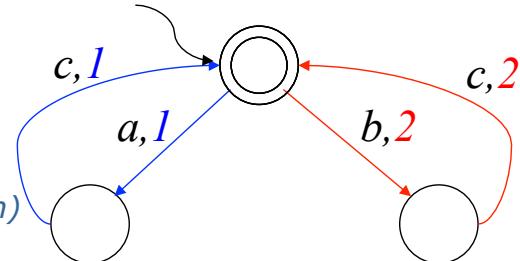
Check: run SAT on PDL formula  $\Phi$

Yes  $\Rightarrow$  (small) model

$\Rightarrow$  extract finite TS

$\Rightarrow$  minimize finite TS

(similar to Mealy machine minimization)



## Results on Synthesizing Composition

- Using PDL reasoning algorithms based on model construction (cf. tableaux), build a (small) model  
*Exponential in the size of the PDL encoding/services finite TS*

*Note: SitCalc, etc. can compactly represent finite TS,  
PDL encoding can preserve compactness of representation*

- From this model extract a corresponding finite TS  
*Polynomial in the size of the model*
- Minimize such a finite TS using standard techniques (opt.)  
*Polynomial in the size of the TS*

*Note: finite TS extracted from the model is not minimal  
because encodes output in properties of individuals/states*

# **Tools for Synthesizing Composition**

- In fact we use only a fragment of PDL in particular we use fixpoint (transitive closure) only to get the universal modality ...
- ... thanks to a tight correspondence between PDLs and Description Logics (DLs), lately highly optimized tableaux based reasoning systems are available to:
  - check for composition existence
  - do composition synthesis (*if the ability of returning models is present*)
- Among them we recall:
  - Racer (<http://www.racer-systems.com/>) based on DLs
  - Pellet (<http://clarkparsia.com/pellet>) based on DLs
  - Fact++ (<http://owl.man.ac.uk/factplusplus/>) based on DLs
  - PDL Tableaux (<http://www.cs.manchester.ac.uk/~schmidt/pdl-tableau/>) based on PDL
  - Tableaux Workbench (<http://twb.rsise.anu.edu.au/>) based on PDL
  - Lotrec (<http://www.irit.fr/Lotrec/>) based on PDL

**Reduction to PDL SAT works also for nondeterministic available services**

# Technique1: Reduction to PDL

Basic idea:

- A orchestrator program  $P$  realizes the target service  $T$  iff at each point:
  - $\forall$  transition labeled  $a$  of the target service  $T$  ...
    - ...  $\exists$  an available service  $B_i$  (the one chosen by  $P$ ) which can make an  $a$ -transition ...
    - ... and  $\forall a$ -transition of  $B_i$  realize the  $a$ -transition of  $T$
- Encoding in PDL:
  - $\forall$  transition labeled  $a$  ...  
use **branching**
  - $\exists$  an available service  $B_i$  ...  
use underspecified predicates **assigned through SAT**
  - $\forall a$ -transition of  $B_i$  ... :  
use **branching** again

# Technical Results: Practical

Reduction to PDL provides also a practical sound and complete technique to compute the orchestrator program also in this case

eg, PELLET @ Univ. Maryland

- Use state-of-the-art tableaux systems for OWL-DL for checking SAT of PDL formula  $\Phi$  coding the composition existence
- If SAT, the tableau returns a finite model of  $\Phi$ 
  - exponential in the size of the behaviors
- Project away irrelevant predicates from such model, and possibly minimize
- The resulting structure is a finite orchestrator program that realizes the target behavior
  - polynomial in the size of the model